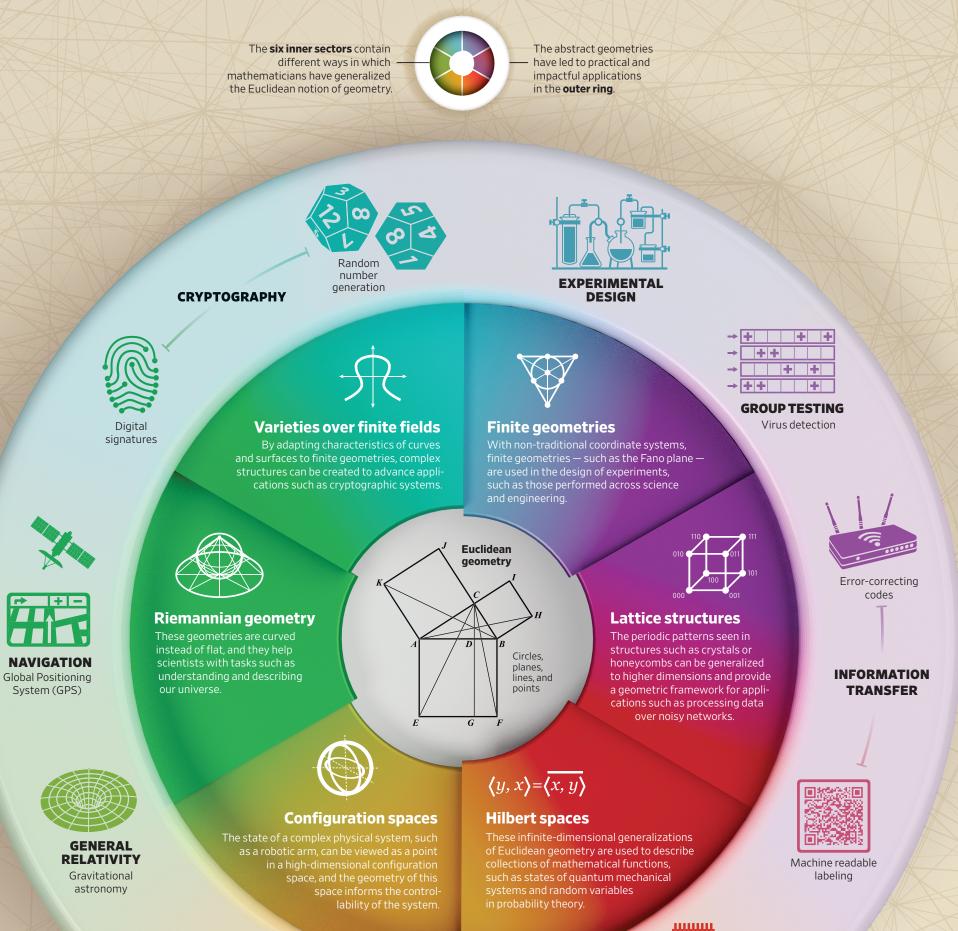
## **Concrete Impacts of Abstract Geometry**

Mathematical theorems that were discovered hundreds of years ago continue to have real-world impact. Euclid, a Greek mathematician who lived around 300 BCE, systematically organized the geometry of points, lines, angles, circles, and planes into the world's first mathematically rigorous theory. Over the past two millennia, mathematicians have expanded upon this with concepts such as curved spaces, discretizations, and dimensions beyond three dimensions. These abstractions have enabled breakthroughs across domains, including data encryption and machine learning.









Quantum computing, electronics

MACHINE LEARNING Computer vision, speech recognition

## [ MODERN SCIENCE AND TECHNOLOGY EMERGE FROM CENTURIES-OLD MATHEMATICAL CONCEPTS ]

NATIONAL ACADEMIES Sciences Engineering Medicine

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